

find the abs. extrema of the function of the given interval.

① $y = 2x^3 + 3x^2 + 12x - 4$ $[-2, 2]$

② $f(x) = \ln(x^2 - 9)$ $[-2, 5]$

Dec 5-9:32 AM

① $y = 2x^3 + 3x^2 + 12x - 4$ $[-2, 2]$

$y' = 6x^2 + 6x + 12$

$0 = 6(x^2 + x + 2)$

$x^2 + x + 2 = 0$

no real sol.

Dec 5-9:39 AM

② $f(x) = \ln(x^2 - 9)$ $[-2, 5]$

$f(x) = \frac{2x}{x^2 - 9} \rightarrow \frac{2x}{(x+3)(x-3)}$

EVT does not apply

$f(x)$ is not continuous in the given interval.

$x \neq \pm 3$ \swarrow 3 is in the interval

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$f(x) = (x^2 - 3)^{2/3}$ $[-3, 2]$

$f'(x) = \frac{2}{3}(x^2 - 3)^{-1/3} (2x)$

$= \frac{4x}{3(x^2 - 3)^{1/3}}$

$4x = 0$
 $x = 0$

$(x^2 - 3)^{1/3} = 0$
 $x^2 - 3 = 0$
 $\sqrt{x^2 - 3} = 0$
 $x = \pm\sqrt{3}$

$f(-3) = 3.302$
 $f(-\sqrt{3}) = 0$
 $f(0) = 2.08$
 $f(\sqrt{3}) = 0$
 $f(2) = 1$

abs Max: 3.302
abs Min: 0

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$f(x) = \sin^2 x + \cos x$ $[0, 2\pi]$

$f(x) = (\sin x)^2 + \cos x$

$f'(x) = 2\sin x \cos x - \sin x$

$0 = \sin x (2\cos x - 1)$

| | |
|---------------------------------|-------------------------|
| $\pi - \theta$ | θ |
| $0, \pi, 2\pi$ | $0, \pi, 2\pi - \theta$ |
| $\frac{\pi}{3}, \frac{5\pi}{3}$ | $\frac{2\pi - \pi}{3}$ |
| | $\frac{\pi}{3}$ |

$\sin x = 0$
 $\cos x = \frac{1}{2}$

$f(0) = 1$ $f(\pi) = -1$

$f(\pi/3) = 1.25$

$f(5\pi/3) = 1.25$

$f(2\pi) = 1$

Min: -1
Max: 1.25

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$f(x) = \frac{2x}{x^2 + 4}$ $[-2, 4]$

$f'(x) = \frac{(x^2 + 4)(2) - 2x(2x)}{(x^2 + 4)^2}$

$= \frac{2x^2 + 8 - 4x^2}{(x^2 + 4)^2} \rightarrow \frac{-2x^2 + 8}{(x^2 + 4)^2}$

$-2x^2 + 8 = 0$
 $-2x^2 = -8$
 $x^2 = 4$
 $x = \pm 2$

$(x^2 + 4)^2 = 0$
 $x^2 + 4 = 0$
 $x^2 = -4$
 $x = \pm 2i$

$f(-2) = -\frac{1}{2}$
 $f(2) = \frac{1}{2}$
 $f(4) = \frac{2}{5}$

Min: $-\frac{1}{2}$
Max: $\frac{1}{2}$

Dec 5-10:06 AM