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Right Triangles
A ladder 20 feet long leans against a vertical house. If the bottom of the ladder slides away from the house horizontally at a rate of 4 ft/sec, how fast is the ladder sliding down the house when the top of the ladder is 8 feet from the ground.

(a) How are these variables related?
 $x^2 + y^2 = z^2$

(b) What is the given information?
 $z = 20$
 $\frac{dx}{dt} = 4$ $y = 8$

(c) What are you looking for?
 $\frac{dy}{dt}$

(d) What is the derivative of this equation?
 $x^2 + y^2 = z^2$
 $2x \frac{dx}{dt} + 2y \frac{dy}{dt} = 2z \frac{dz}{dt}$
 $2(\sqrt{336})(4) + 2(8) \frac{dy}{dt} = 2(20)(0)$
 $8\sqrt{336} + 16 \frac{dy}{dt} = 0$
 $\frac{dy}{dt} = -\frac{8\sqrt{336}}{16}$
 $\frac{dy}{dt} = -\frac{\sqrt{336}}{2}$ ft/sec

(e) What is x at this time?
 $x = \sqrt{336}$

Advice from Mr. C:

- 1) Since the length of z does not change, $\frac{dz}{dt} = 0$
- 2) Remember, not to plug the variables until you find the derivative
- 3) Then go back to the original $x^2 + y^2 = z^2$, to find the missing side of the right triangle

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Cylinder

The volume of a right circular cylinder is $V = \pi r^2 h$

If the cylinder does not change dimensions and water is poured in what happens to

(a) $\frac{dh}{dt}$ of the water (b) $\frac{dr}{dt}$ of the water

1) A right cylindrical tank is filled with water. The tank stands upright has radius 20 cm. How fast does the height of water in the tank drop when the water is being drained at 25 cm³/sec?

2. Given Information:
 $r = 20$
 $\frac{dV}{dt} = -25$

3. Looking for:
 $\frac{dh}{dt}$

4. The derivative of the equation:
 $V = \pi r^2 h$
 $\frac{dV}{dt} = \pi r^2 \frac{dh}{dt} + 2\pi r \frac{dr}{dt} h$
 $-25 = \pi (20)^2 \frac{dh}{dt}$
 $-25 = 400\pi \frac{dh}{dt}$
 $-\frac{1}{16}\pi \text{ cm/sec} = \frac{dh}{dt}$

Advice from Mr. C:

1. When taking the derivative of the volume equation use the product rule and think of the equation as $V = (\pi r^2)(h)$
2. Remember, if the cylinder does not change dimensions, the radius of the substance inside will not change, hence $\frac{dr}{dt} = 0$