

Geometry CC - Unit 4  
Lesson 3: Rotations  
MS.1.12

Name: \_\_\_\_\_  
Date: \_\_\_\_\_

**Rotation [Turn]**  
Transformation around a center of rotation with a specific angle of rotation and in a certain direction (clockwise or counterclockwise).

Each point of the preimage and the image are the same distance from the center.

Apply each reflection to the point given

$P(2, 3)$

x-axis  $(2, -3)$   
y-axis  $(-2, 3)$   
 $y = x$   $(3, 2)$   
 $y = -x$   $(-3, -2)$   
 $R_{90^\circ}$   $(-3, 2)$   
 $R_{180^\circ}$   $(-2, -3)$   
 $R_{270^\circ}$   $(3, -2)$

Oct 22-11:52 AM

**Exploring Rotations**  
<http://www.geogebra.org/m/9m1559>

**Example 1:**  
Graph JKLM on the coordinate plane. Give the coordinates of the image if B is rotated  $90^\circ$  counter-clockwise about the origin.

Rotation  $90^\circ$  counter-clockwise about the origin  
 $(x, y) \rightarrow (-y, x)$

Image Coordinates:  
 $B(2, 3) \rightarrow B'(-3, 2)$

**Example 2:**  
Graph JKLM on the coordinate plane where  $J(-2, 1)$ ,  $K(-1, 4)$ , and  $M(-2, 4)$ . Give the coordinates of the image if JKLM is rotated  $180^\circ$  counter-clockwise about the origin.

Rotation  $180^\circ$  counter-clockwise about the origin  
 $(x, y) \rightarrow (-x, -y)$

Image Coordinates:  
 $J(-2, 1) \rightarrow J'(2, -1)$   
 $K(-1, 4) \rightarrow K'(1, -4)$   
 $L(3, 4) \rightarrow L'(-3, -4)$   
 $M(3, 1) \rightarrow M'(-3, -1)$

**Example 3:**  
Graph L(4, 2) on the coordinate plane. Give the coordinates of the image if L is rotated  $270^\circ$  counter-clockwise about the origin.

Rotation  $270^\circ$  counter-clockwise about the origin  
 $(x, y) \rightarrow (y, -x)$

Image Coordinates:  
 $L(4, 2) \rightarrow L'(2, -4)$

**Summary of  $90^\circ$ ,  $180^\circ$ , and  $270^\circ$  rotations about the origin:**

Rotation  $90^\circ$  counterclockwise about the origin  
 $(x, y) \rightarrow (-y, x)$

Rotation  $180^\circ$  counterclockwise about the origin  
 $(x, y) \rightarrow (-x, -y)$

Rotation  $270^\circ$  counterclockwise about the origin  
 $(x, y) \rightarrow (y, -x)$

What about  $360^\circ$  rotations?  
The pre-image would make a circle.  
Can you keep rotating in  $90^\circ$  increments past  $360^\circ$ ?  
Yes ex.  $450 - 360 = 90$

Will these rules hold if the center of rotation is not the origin? Why?  
NO

**Example 4:**  
Name the coordinates of the vertices of the image after the given rotation and then graph the image. You do not have to use any tools to complete this process.

$90^\circ$  counterclockwise about the origin

Preimage:  $Q(1, 1)$ ,  $R(4, 5)$ ,  $S(2, 2)$   
Image:  $Q'(-1, 1)$ ,  $R'(-5, 4)$ ,  $S'(-2, 5)$

**Example 5:**  
Name the coordinates of the vertices of the image after the given rotation and then graph the image. You do not have to use any tools to complete this process.

$170^\circ$  counterclockwise about the origin

Preimage:  $A(-4, 0)$ ,  $B(-2, 2)$ ,  $C(-3, -5)$   
Image:  $A'(0, 4)$ ,  $B'(-2, 2)$ ,  $C'(-6, 3)$

Example 6:  
Name the coordinates of the vertices of the image after the given rotation and then graph the image. You do not have to use any tools to complete this process.

180° rotation about the origin

Preimage	Image
W(-3, -3)	→ W' (3, 3)
X(3, -4)	→ X' (-3, 4)
Y(4, 1)	→ Y' (-4, -1)
Z(-5, 4)	→ Z' (5, -4)